Exponential Functions (2023-2024)

SCORE:

Name ______ Date _____ Period _____

Approximate the value using a calculator. Express answer rounded to three decimal places.

1.
$$5^{2.71}$$

2.
$$e^{3.14}$$

$$3. 2.1^3$$

The graph of an exponential function is given. Match the graph to one of the following functions. Use transformations to find the answers. Do not use a calculator.

a)
$$y = 3^{1}$$

b)
$$y = 3^{-x}$$

c)
$$y = -3^{x}$$

a)
$$y = 3^x$$
 b) $y = 3^{-x}$ c) $y = -3^x$ d) $y = -3^{-x}$

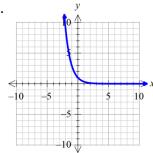
e)
$$y = 3^x - 1$$

$$f$$
) $y = 3^{x-1}$

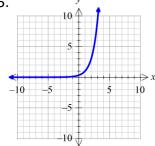
$$(g) y = 3^{1-x}$$

e)
$$y = 3^{x} - 1$$
 f) $y = 3^{x-1}$ g) $y = 3^{1-x}$ h) $y = 1 - 3^{x}$

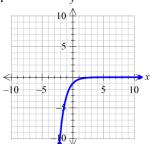
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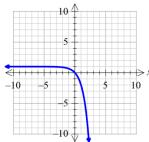
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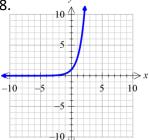
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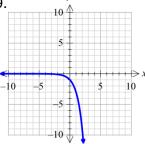
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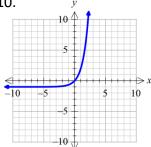
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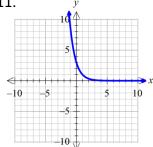
9.



10.



11.



Use transformations and 3 key points to graph each function. Determine the domain, range, and horizontal asymptote of each function. Use a table! No Graphing Calculator! Show work!

12.
$$f(x) = 2^x + 1$$

Domain: _____

Asymptotes:_____

Key points and transformations:

х	f(x)

х	f(x)

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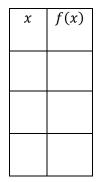
Range: _____

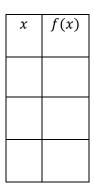
13.
$$f(x) = -3^{x-1}$$

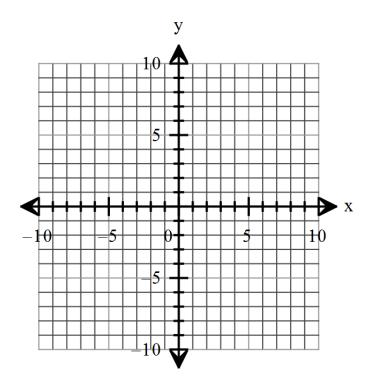
Domain: _____

Asymptotes:_____

Key points and transformations:







Range: ______

14.
$$f(x) = 3^{x/2} + 2$$

Domain: _____

Asymptotes:_____

Key points and transformations:

х	f(x)

x	f(x)

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Range: _____

15.
$$f(x) = 2^{-x} - 3$$

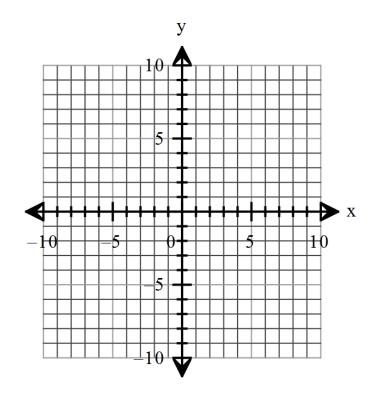
Domain: _____

Asymptotes:_____

Key points and transformations:

x	f(x)

х	f(x)



Range: _____

Solve each equation using the one-to-one property for exponents. Show work! You may need to factor to solve.

16.
$$7^x = 7^3$$

17.
$$\left(\frac{1}{4}\right)^x = \frac{1}{64}$$

18.
$$3^{-x} = 81$$

19.
$$4^{x^2} = 2^x$$

20.
$$9^{-x+15} = 27^x$$

21.
$$4^x \cdot 2^{x^2} = 16^2$$

Find the amount that results from each investment. Round answers to the nearest cent.

Compounded Interest: $A = P(1 + \frac{r}{n})^{nt}$ P = Initial amount or Principle, r = rate, n = number of times in a year, t = time in years, A = the total amount with interest

22. \$100 invested at 4% compounded guarterly after a period of 2 years.

23. \$1000 invested at 11% compounded monthly after a period of 2 years.

Review Exercises

Find the domain of the given functions. Write answers in interval notation. Show work!

24.
$$f(x) = \frac{x+2}{(x-3)(x+5)}$$

25.
$$f(x) = \sqrt{-2x+7}$$