Name $\qquad$ Date $\qquad$ Period $\qquad$

Evaluate the limit and end behavior based on the graph of $f(x)$ shown.

1. $\lim _{x \rightarrow 5^{+}} f(x)=$

$$
\lim _{x \rightarrow 5^{-}} f(x)=
$$

$\lim _{x \rightarrow \infty} f(x)=$
$\lim _{x \rightarrow-\infty} f(x)=$

2. $\lim _{x \rightarrow-1^{+}} f(x)=\quad \lim _{x \rightarrow-1^{-}} f(x)=$

$$
\begin{array}{ll}
\lim _{x \rightarrow \infty} f(x)= & \lim _{x \rightarrow-\infty} f(x)= \\
\lim _{x \rightarrow 2^{+}} f(x)= & \lim _{x \rightarrow 2^{-}} f(x)=
\end{array}
$$



Find the vertical asymptote(s) (remember it is the same as the restrictions, set the denominator $=0$ and solve for $\boldsymbol{x}$ ).
3. $f(x)=\frac{1}{x+4}$
Vertical
Asymptote(s): $\qquad$

Show Work:
4. $f(x)=\frac{x}{x-2}$

Vertical
Asymptote(s): $\qquad$
Show Work:
5. $f(x)=\frac{x+1}{(2 x-1)(x+3)}$

Vertical
Asymptote(s): $\qquad$
Show Work:

Find the restrictions. Use the restrictions to find the domain. Write the domain in interval notation (remember the vertical asymptote(s) are the same as the restrictions).
6. $f(x)=\frac{1}{x-5}$
7. $f(x)=\frac{x}{3 x+2}$
8. $f(x)=\frac{x+2}{(x-1)(4 x+3)}$

Restriction: $\qquad$
Domain: $\qquad$
Show Work:
Show Work:
$\qquad$ Restriction: $\qquad$

Domain: $\qquad$
Show Work:

Find the horizontal asymptotes and the $\boldsymbol{x}$-intercept.
9. $f(x)=\frac{1}{3 x+1}$
10. $f(x)=\frac{x}{x-6}$
11. $f(x)=\frac{x-4}{(2 x-5)(x-7)}$

Horizontal
Asymptote: $\qquad$
$x$-intercept(s): $\qquad$
Show Work:

Horizontal
Asymptote: $\qquad$

Horizontal Asymptote: $\qquad$
$x$-intercept(s): $\qquad$ $x$-intercept(s): $\qquad$
Show Work:
Show Work:

Find the $\boldsymbol{y}$-intercepts (make $\boldsymbol{x}=0$ and solve).
12. $f(x)=\frac{1}{x+4}$
13. $f(x)=\frac{x}{x-2}$
$y$-intercept: $\qquad$ Show Work:

Show Work:

Find the parts of a rational function asked for below.
15. $f(x)=\frac{2 x-3}{x^{2}+8 x+15}$

Vertical
Asymptote(s): $\qquad$
$x$-intercept(s): $\qquad$

Factored form:

Horizontal
Asymptote: $\qquad$
$y$-intercept(s): $\qquad$ Work:

Given the graph of the function below, determine the key features.

$y$-intercept: $(0,-4.11) \quad x$-intercept(s): $(-1.03,0)$, $(2.66,0),(3.37,0)$

Domain: Range:

Positive:

Negative:

Increasing:

Decreasing:

Maximums / minimums:

End Behavior/Limits:

$$
\begin{array}{ll}
\lim _{x \rightarrow-\infty} f(x)= & \lim _{x \rightarrow \infty} f(x)= \\
\lim _{x \rightarrow-1^{-}} f(x)= & \lim _{x \rightarrow-1^{+}} f(x)= \\
\lim _{x \rightarrow 3^{-}} f(x)= & \lim _{x \rightarrow 3^{+}} f(x)=
\end{array}
$$

Vertical Asymptote(s): Horizontal Asymptote:

