8.6

Date:

Objective:

Review: Find the exact values of all 6 trigonometric functions. Write answer in simplest form.


| $\sin A=$ | $\cos A=$ |
| :--- | :--- |
| $\tan A=$ | $\sec A=$ |
| $\csc A=$ | $\cot A=$ |

Find the degree measure of $\theta$ in the above triangle.

## Vocabulary:

Standard position:

Initial side:

Terminal side:

Reference angle:

What if I put the above triangle in standard position in the first quadrant?

What is the $x$-coordinate?
What is the $y$-coordinate?
What is the hypotenuse?
$\sin A=$
$\sec A=$
$\csc A=$
$\cot A=$


What do you notice about the signs of the $x$ - and $y$-corrodinates and the 6 trig functions?

Now do the same thing with the triangle in the second quadrant.

What is the $x$-coordinate?

What is the $y$-coordinate?

What is the hypotenuse?

$\sin A=\quad \cos A=\quad \tan A=\quad \csc A=\quad \cot A=$

What do you notice about the signs of the $x$ - and $y$-corrodinates and the 6 trig functions?

How about the third quadrant?

What is the $x$-coordinate?

What is the $y$-coordinate?

What is the hypotenuse?

$\sin A=$
$\cos A=$
$\tan \mathrm{A}=$
$\sec A=$
$\csc A=$
$\cot A=$

What do you notice about the signs of the $x$ - and $y$-corrodinates and the 6 trig functions?

How about the fourth quadrant?

What is the $x$-coordinate?

What is the $y$-coordinate?

What is the hypotenuse?

$\sin A=$
$\cos A=$
$\tan \mathrm{A}=$
$\sec A=$
$\csc A=$
$\cot A=$

What do you notice about the signs of the $x$ - and $y$-corrodinates and the 6 trig functions?

What side does the $x$-coordinate equal on a right triangle with $\theta$ at the origin?
What side does the $y$-coordinate equal on a right triangle with $\theta$ at the origin?
Write the 6 trig functions using $x, y, h$ instead of opposite, adjacent, hypotenuse.
$\sin \mathrm{A}=\cos \mathrm{A}=\quad \tan \mathrm{A}=\quad \sec \mathrm{A}=\quad \csc \mathrm{A}=\quad \cot \mathrm{A}=$

The signs of the trigonometric functions depend on the quadrant in which the angle lies and the corresponding signs of $x$ and $y$ (remember $r$ is always positive).

A good mnemonic to remember which functions are positive in each quadrant is "All Students Take Calculus".
Quadrant I:

Quadrant II:

Quadrant III:
Quadrant IV:


## Examples:

Find the exact values of $\sin \theta, \cos \theta, \tan \theta, \csc \theta, \sec \theta$, and $\cot \theta$ where $\theta$ is an angle in standard position whose terminal side contains the given point. Write answers in simplest form.

1. $(-1,3)$

$\sin \theta=$ $\qquad$ $\csc \theta=$ $\qquad$
$\cos \theta=$ $\qquad$ $\sec \theta=$ $\qquad$
$\tan \theta=$ $\qquad$ $\cot \theta=$ $\qquad$

Find the degree of the angle (round to the nearest tenth of a degree), in standard position, whose terminal side contains the given point.
2. $(3,8)$
$\theta=$ $\qquad$


REMEMBER: There are 2 quadrants where each trig function is positive and 2 quadrants where each trig function is negative.

Draw the two triangles for the trig functions and find the coordinates that go with it. There will be 2 answers. Leave answers in simplest radical form. (Remember All Students Take Calculus). Then find the angles from [ $0,360^{\circ}$ ) in standard position (round to the nearest tenth of a degree).
3. $\sin \theta=-\frac{2}{7}$


Coordinates: $\qquad$ and $\qquad$

4. $\cos \theta=\frac{24}{25}$

Coordinates: $\qquad$ and $\qquad$


Angles: $\qquad$ and $\qquad$

5. $\tan \theta=-\frac{2}{5}$

Coordinates: $\qquad$ and $\qquad$ Angles: $\qquad$ and $\qquad$




