

9.1

Date:

Objective:

Finding Sine, Cosine, and Tangent on the Unit Circle

You can use the (x,y) coordinates on the unit circle to solve for the sin, cos, and tan.

$$\sin \theta = \frac{opp}{hyp} = \frac{y}{1} = y$$

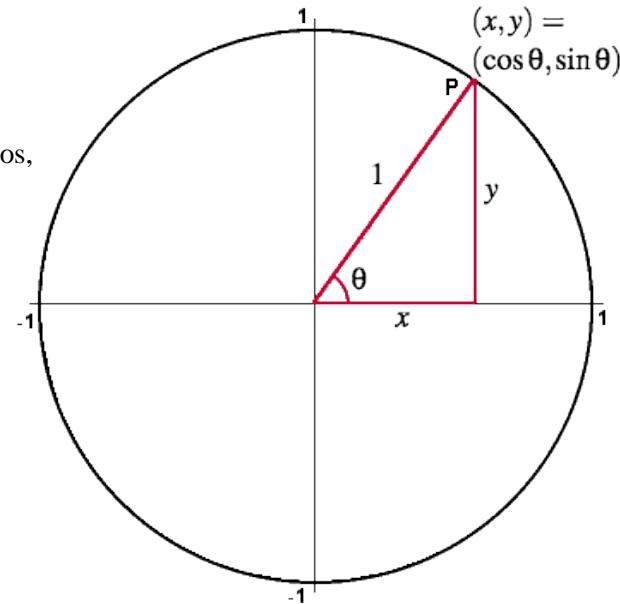
$$\cos \theta = \frac{adj}{hyp} = \frac{x}{1} = x$$

$$\tan \theta = \frac{opp}{adj} = \frac{y}{x}$$

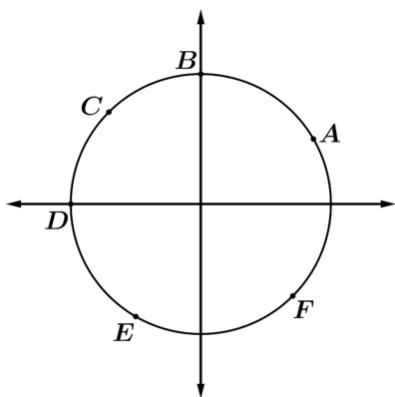
$$\csc \theta = \frac{hyp}{opp} = \frac{1}{y}$$

$$\sec \theta = \frac{hyp}{adj} = \frac{1}{x}$$

$$\cot \theta = \frac{adj}{opp} = \frac{x}{y}$$



Example: Refer to the diagram below. For the indicated point, tell if the value for each trigonometric function is **positive, negative, neither (zero), or undefined**. Write the value of the trig function using **x** and/or **y**.



a) $\sin A$

Pos, Neg, Zero, or Und?

Value: _____

b) $\cos C$

Pos, Neg, Zero, or Und?

Value: _____

c) $\tan C$

Pos, Neg, Zero, or Und?

Value: _____

d) $\cot D$

Pos, Neg, Zero, or Und?

Value: _____

e) $\tan D =$

Pos, Neg, Zero, or Und?

Value: _____

f) $\sec F =$

Pos, Neg, Zero, or Und?

Value: _____

State the angle in **degrees** represented by the given coordinate point.

1. $\left(\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$

2. $(-1, 0)$

3. $\left(-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$

State the angle in **radians** represented by the given coordinate point.

1. $\left(\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$

2. $(0, 1)$

3. $\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$

Practice: Draw the angle. Use the unit circle to identify the requested trig ratios.

1. $\sin 30^\circ = \underline{\hspace{2cm}}$

3. $\sin -\frac{\pi}{3} = \underline{\hspace{2cm}}$

$\cos 30^\circ = \underline{\hspace{2cm}}$

$\cos -\frac{\pi}{3} = \underline{\hspace{2cm}}$

$\tan 30^\circ = \underline{\hspace{2cm}}$

$\tan -\frac{\pi}{3} = \underline{\hspace{2cm}}$

2. $\sin -150^\circ = \underline{\hspace{2cm}}$

4. $\sin \frac{\pi}{2} = \underline{\hspace{2cm}}$ $\csc \frac{\pi}{2} = \underline{\hspace{2cm}}$

$\cos -150^\circ = \underline{\hspace{2cm}}$

$\cos \frac{\pi}{2} = \underline{\hspace{2cm}}$ $\sec \frac{\pi}{2} = \underline{\hspace{2cm}}$

$\tan -150^\circ = \underline{\hspace{2cm}}$

$\tan \frac{\pi}{2} = \underline{\hspace{2cm}}$ $\cot \frac{\pi}{2} = \underline{\hspace{2cm}}$

Find the exact value of each trig function using the unit circle as a reference.

1. $\tan \pi$

2. $\cot \pi$

3. $\csc 150^\circ$

4. $\csc -150^\circ$

5. $\sec 30^\circ$

6. $\sec \frac{3\pi}{4}$

7. $\csc 180^\circ$

8. $\sec \frac{3\pi}{2}$