Objective:

## Analyze the graph

Domain:
Range:
$x$-intercept(s):
$y$-intercept:
Relative or local maximum point(s):
Relative or local maximum value(s):
Relative or local minimum point(s):
Relative or local minimum value(s):
Absolute maximum point(s):
Absolute maximum value(s):
Absolute minimum point(s):
Absolute minimum value(s):
Increase interval:
Decrease interval:
Constant interval:
Positive interval:
Negative interval:
Symmetry:
End behavior: $\quad \lim _{x \rightarrow \infty} f(x)=\quad \lim _{x \rightarrow-\infty} f(x)=$

## Find symmetry algebraically

Even--- $f(x)=f(-x)$
$\operatorname{Odd}---f(x)=f(-x)$

Example:
$f(x)=2 x^{4}-3 x^{2}+4$


Types of symmetry:


$$
f(x)=-2 x^{7}-5 x^{5}+7 x^{3}+2
$$

A)

B)

a) At what number(s), if any, does $f$ have a local maximum?
b) What are the local maxima?
c) At what number(s), if any, does $f$ have a local minimum?
d) What are the local minima?
e) List the intervals where $f$ is increasing and the intervals where $f$ is decreasing.
f) List the intervals where $f$ is positive and the intervals where $f$ is negative.

## Find the Average Rate of Change of a Function

To find the average rate of change of a function between any two points on its graph, calculate the slope of the line containing the two points.

If $a$ and $b, a \neq b$, are in the domain of a function $y=f(x)$, the average rate of change of $\boldsymbol{f}$ from $a$ to $b$ is defined as:

Average rate of change $=\frac{\Delta y}{\Delta x}=\frac{f(b)-f(a)}{b-a} \quad a \neq b$

The symbol $\Delta y$ above is "the change in $y$," and $\Delta x$ is the "change in $x$." The average rate of change of $f$ is the change in $y$ divided by the change in $x$.

## Example:

Find the average rate of change of $f(x)=3 x^{2}$ for the following intervals:
a) From 1 to 3 or $[1,3]$
b) From 1 to 5 or $[1,5]$
c) From 1 to 7 or $[1,7]$
d)

| Years | Cost |
| :---: | :---: |
| 1 | 2 |
| 2 | 3 |
| 3 | 5 |
| 4 | 8 |
| 5 | 9 |

[2,5]

