

Date: 12/5/23

Section: 4.5

Objective: I can find the inverse of a function.

Vocabulary:

Inverse: opposite

Inverse operation: operation that undo each other

Inverse property: opp. property

One-to-one property: Both $f(x)$ & $f^{-1}(x)$ are functions

Way to find one-to-one:

Pass VLT & HLT

To find the inverse using a table: flip-flop x & y To find the inverse using ordered pairs:

Example 1:

$f(x)$		$f^{-1}(x)$	
x	y	x	y
5	5	5	5
7.5	6	6	7.5
-9	-8	-8	-9
15	-5	-5	15
-2	3	3	-2

inverse notation

Example 2:

$\{(1,1), (2,4), (3,9), (0,0), (-1,1), (-2,4)\}$

$\{(1,1), (4,2), (9,3), (0,0), (1,-1), (4,-2)\}$

To find the inverse using a graph: WAY 1)

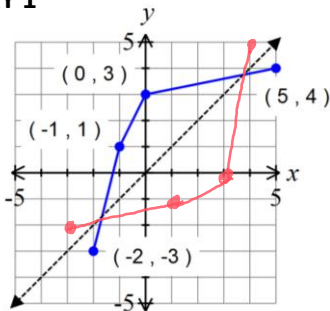
find some ordered & flip-flop them

WAY 2)

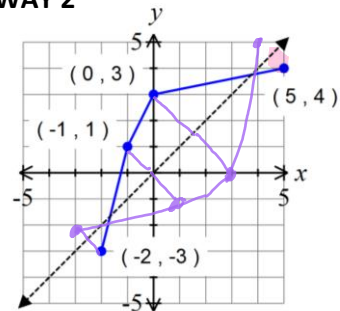
reflecting over $y=x$

Example 3:

WAY 1



WAY 2



Which of the above examples, #1, #2, or #3, are one-to-one and why?

1 & 3

Which parent graph is not one-to-one without restrictions?

To find the inverse using an equation:

- ① flip-flop x & y
- ② solve y

Find the inverse function, domain, and range.

Example 1: $f(x) = y$

$$f(x) = -3x + 1 \quad (-\infty, \infty) \xrightarrow{\text{becomes } R \text{ \& } \text{inverse}} \mathbb{R}$$

$$x = -3y + 1$$

$$x - 1 = -3y$$

$$\frac{x-1}{-3} = f^{-1}(x) \quad D = (-\infty, \infty) \\ R = (-\infty, \infty)$$

Example 3:

$$f(x) = \sqrt[3]{x+2} - 3$$

- Prove show All work

To verify that two functions are inverses, show that

$$(f \circ g)(x) = (g \circ f)(x) = x$$

Example 1:

Verify that the inverse of $f(x) = \frac{2}{x+5}$ is $f^{-1}(x) = \frac{2}{x} - 5$.

Example 2:

$$f(x) = -2\sqrt{3-x}$$

$$x = -2\sqrt{3-y}$$

$$\frac{x}{-2} = \sqrt{3-y}$$

$$\frac{x^2}{4} = 3-y$$

$$\frac{x^2}{4} - 3 = -y$$

Example 4:

$$f(x) = \frac{2x+3}{5x-4}$$

$$x = \frac{2y+3}{5y-4}$$

$$5xy - 4x = 2y + 3$$

$$5xy - 2y = 4x + 3$$

$$y(5x-2) = 4x+3$$

$$3-x \geq 0 \\ -x \geq -3 \\ x \leq 3 \\ D = (-\infty, 3] = x$$

$$f^{-1}(x) = -\frac{x^2}{4} + 3 \\ D = (-\infty, \infty) \\ R = (-\infty, 3] = y$$

$$D = (-\infty, \frac{4}{3}) \cup (\frac{4}{3}, \infty)$$

$$f^{-1}(x) = \frac{4x+3}{5x-2} \\ D = (-\infty, \frac{2}{5}) \cup (\frac{2}{5}, \infty) \\ R = (-\infty, \frac{4}{3}) \cup (\frac{4}{3}, \infty)$$

Example 2:

Verify that the inverse of $f(x) = \sqrt[3]{2x}$ is $f^{-1}(x) = \frac{x^3}{2}$.

$$(f \circ g)(x)$$

$$\sqrt[3]{2(\frac{x^3}{2})}$$

$$\sqrt[3]{x^3}$$

x

they are inverses

$$(g \circ f)(x)$$

$$\frac{(\sqrt[3]{2x})^3}{2}$$

$$\frac{2x}{2}$$

x