

4.5 Inverse Functions

Name _____ Period _____ Date _____

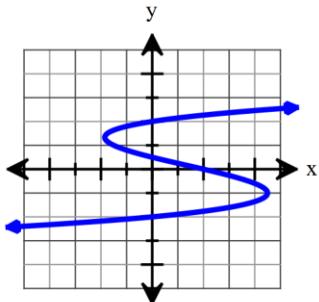
Determine whether the function is one-to-one.

1. $\{(-2, 5), (-1, 3), (3, 7), (4, 12)\}$

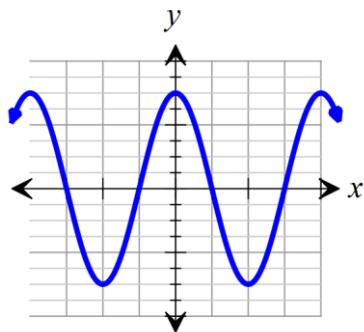
2. $\{(2, 6), (-3, 6), (4, 9), (1, 10)\}$

In each exercise determine a) whether the relation is a function and b) whether the relations inverse is a function.

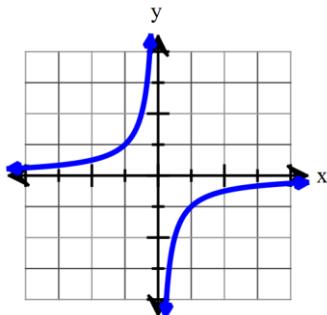
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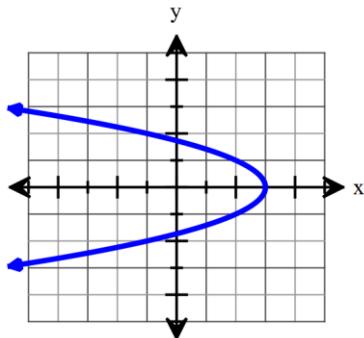
4.



5.



6.

**Find the inverse of each one-to-one function, then state the domain and range of each inverse function.**

7. $\{(-2, 2), (-1, 6), (0, 8), (1, -3), (2, 9)\}$

8. $\{(-2, -8), (-1, -1), (0, 0), (1, 1), (2, 8)\}$

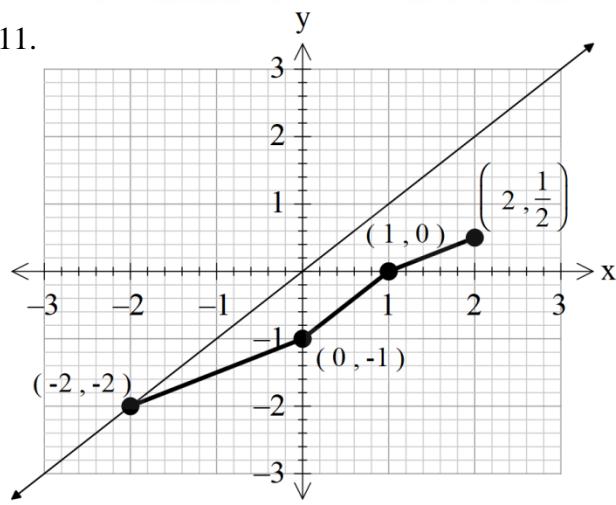
Confirm that f and g are inverses by showing that $f(g(x)) = x$ and $g(f(x)) = x$. Give any values of x that need to be excluded from the domain of f and the domain of g . Show work!

9. $f(x) = 3x - 2$ and $g(x) = \frac{x+2}{3}$

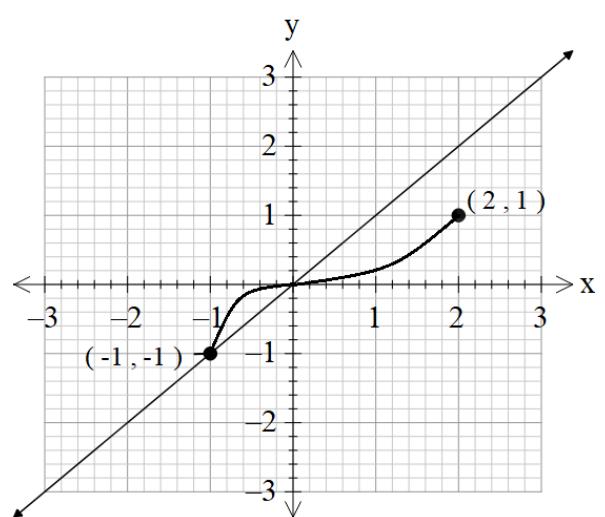
10. $f(x) = x^3 + 1$ and $g(x) = \sqrt[3]{x-1}$

The graph of a one-to-one function f is given. Draw the graph of the inverse function f^{-1} .
The graph of $y = x$ is also given for convenience.

11.



12.



The function f is one-to-one. Find its inverse and domain. Show work!

13. $f(x) = 3x - 6$

Domain:

14. $f(x) = 2x + 5$

Domain:

15. $f(x) = \frac{2x-3}{x+1}$

Domain:

16. $f(x) = \frac{x+3}{x-2}$

Domain:

17. $f(x) = \sqrt{x-2}$

Domain:

18. $f(x) = \sqrt{x+5}$

Domain:

19. $f(x) = x^3 + 4$

Domain:

20. $f(x) = \sqrt[3]{x+3} - 2$

Domain:

21. $f(x) = (x-1)^3 + 6$ Domain:

22. $f(x) = \frac{1}{2}\sqrt{x-1} - 3$ Domain:

Use the table to write the table for the inverse function.

23.

x	$f(x)$
0	4
2	2
4	-4
6	-14
8	-28

x	$f^{-1}(x)$

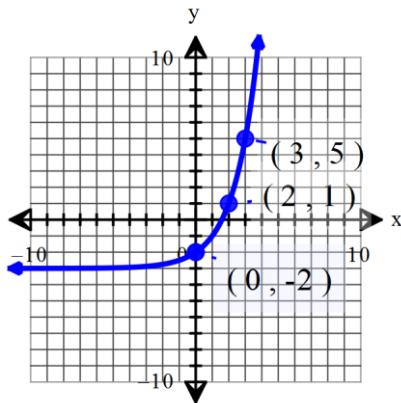
24.

x	$f(x)$
-17	1.7
-12	1.6
-9	1.5
-7	1.4
-3	1

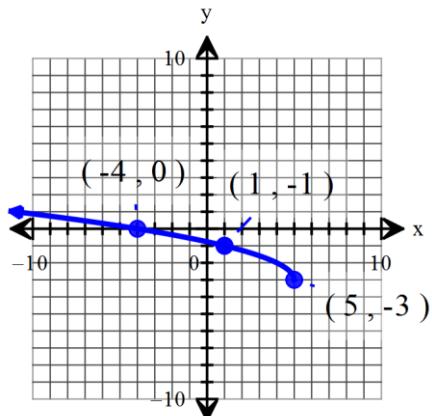
x	$f^{-1}(x)$

Use the graph to draw the graph to the inverse function.

25.



26.



27. Use the graph from problem 25 to evaluate the following:

- a) $f(2)$ b) $f(1)$ c) $f^{-1}(0)$ d) $f^{-1}(-1)$

28. If $f(7) = 13$ and f is one-to-one, what is $f^{-1}(13)$?

29. The domain of a one-to-one function g is $(-\infty, 0]$, and its range is $[0, \infty)$. State the domain and the range of g^{-1} .

30. A function $y = f(x)$ is increasing on the interval $(0, 5)$. What conclusion can you draw about the graph of $y = f^{-1}(x)$?

31. A function f has an inverse function. If the graph of f lies in quadrant I, in which quadrant does the graph of f^{-1} lie?

Review Exercises

Multiply the polynomials. Show work!

$$32. (x-7)(x+7)$$

$$33. (x-7)^2$$

$$34. (x+7)^2$$

35. Write the polynomial in factored form with zeros of -4, 2, 0.

36. Divide using synthetic division.
$$\frac{2x^4 - 3x^2 - 5x + 10}{x - 2}$$

37. Factor. $20x^2 - 45y^2$