

Date: 2/22/24 Section: 7.1

Objective: I can use The law of sines to find angles and sides of triangles.

Starter: (Round answers to the nearest tenth.)

1. Solve for x.

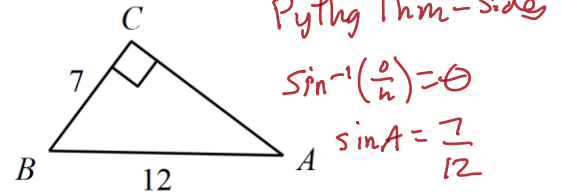
$$\frac{2}{6} = \frac{3}{x+7}$$

$$3\left(\frac{6}{2} = \frac{x+7}{3}\right)$$

$$9 = x+7$$

$$x = 2$$

2. Find the measure of the angle indicated.

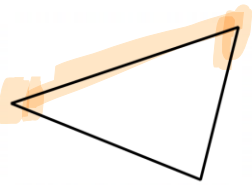


When do you use sine, cosine, and tangent to solve for a missing side or angle of a triangle?

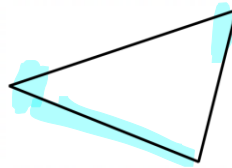
What happens if the triangle is an oblique triangle? *oblique means not right triangle*An oblique triangle is a triangle without a right angle. To solve an oblique triangle, we must know three pieces of information, at least one of which must be the length of a side. (Three angles define an infinite number of triangles).**A. Law of Sines –**

**Use when you have ASA, AAS, or SSA

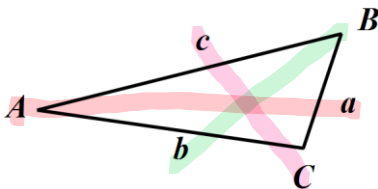
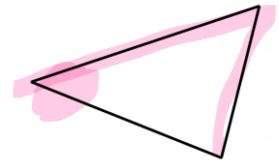
ASA triangle



AAS triangle



SSA triangle (ambiguous case)



Law of sines:

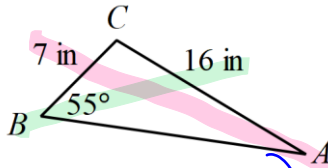
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \quad \text{--- to find sides}$$

or

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c} \quad \text{--- to find angles}$$

Examples: Identify the type of triangle. Then find each measurement indicated using law of sines. Round your answers to the nearest tenth.

1. Find $m\angle A$ *SSA*



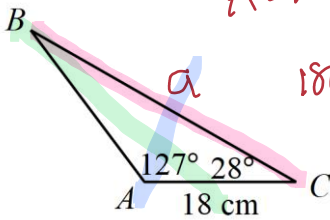
$m\angle A = 21.0^\circ$

$$\left(\frac{\sin A}{7} = \frac{\sin 55^\circ}{16} \right)$$

~~$\sin A = \frac{7 \sin 55^\circ}{16}$~~

$\sin^{-1}\left(\frac{7 \sin(55)}{16}\right)$

3. Find BC



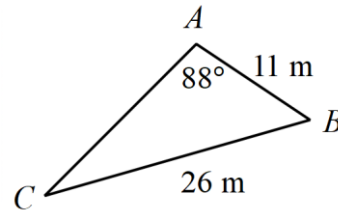
ASA

$180^\circ - 127^\circ - 28^\circ = 25^\circ$

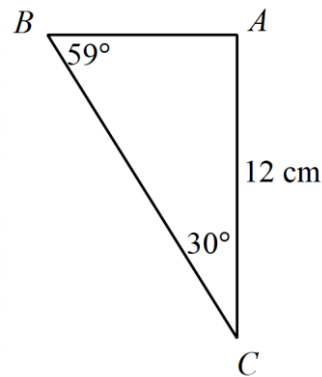
$$\left(\frac{a}{\sin 127^\circ} = \frac{18}{\sin 25^\circ} \right) \sin 127^\circ$$

$a \approx 34.0 \text{ cm}$

2. Find $m\angle C$ *SSA*



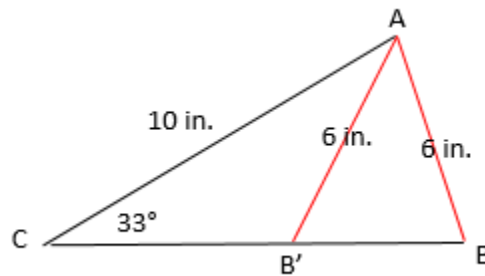
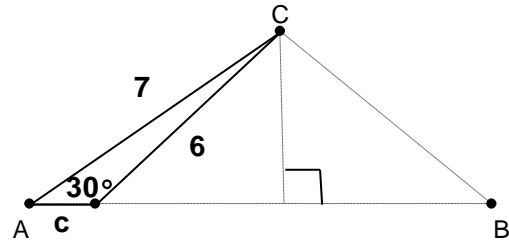
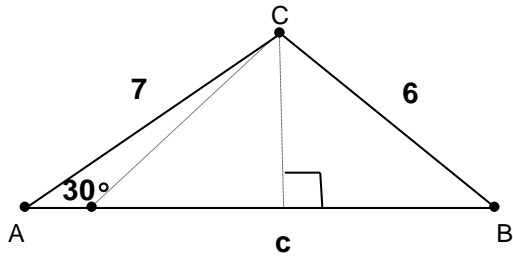
4. Find AB



If the picture is not draw for an SSA triangle, you do not know how the triangle is put together.

SSA (The Ambiguous Case): If you know two sides and a non-included angle (an angle that is not between the sides), there may be zero, one, or two possible triangles that fit the given measurements.

Solve $\triangle ABC$ given that $a = 6$, $b = 7$, and $\angle A = 30^\circ$. Two triangles are possible with the given information.



To determine if there is a 2nd valid angle:

1. See if you are given two sides and the angle not in between (SSA). This is the situation that may have 2 possible answers.
2. Find the value of the unknown angle.
3. No triangle: *error*

One triangle: *found angle < given angle*

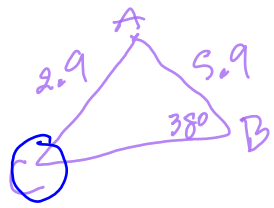
Two triangles: *found > given angle*

****When using law of sines, you must _____!!!!!!!!

Examples:

SSA

a) $B = 38^\circ, b = 2.9, c = 5.9$

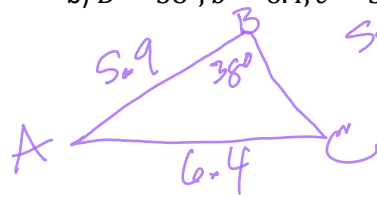


$$\left(\frac{\sin C}{5.9} = \frac{\sin 38^\circ}{2.9} \right) 5.9$$

$$\sin^{-1} \left(\frac{5.9 \sin 38^\circ}{2.9} \right) = C$$

NO triangle

b) $B = 38^\circ, b = 6.4, c = 5.9$



$$\left(\frac{\sin C}{5.9} = \frac{\sin 38^\circ}{6.4} \right) 5.9$$

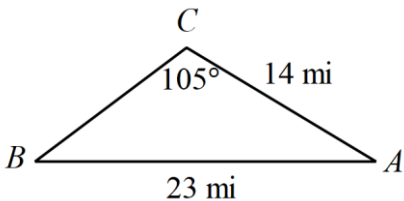
$$\sin^{-1} \left(\frac{5.9 \sin 38^\circ}{6.4} \right) = C$$

$C \approx 34.58^\circ$

$34.58^\circ < 38^\circ$
so only 1 triangle

Examples: Solve each triangle. Round your answers to the nearest tenth. Hint: Draw the triangle and identify the type of triangle.

1.



$m\angle A = 39.0^\circ$ $a = 15.0 \text{ mi}$

$m\angle B = 36.0^\circ$ $b = 14 \text{ mi}$

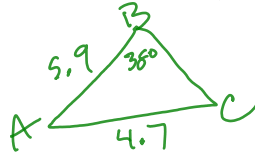
$m\angle C = 105^\circ$ $c = 23 \text{ mi}$

$$\left(\frac{\sin B}{14} = \frac{\sin 105^\circ}{23} \right) 14$$

$$\sin^{-1} \left(\frac{14 \sin 105^\circ}{23} \right)$$

$$\left(\frac{a}{\sin 39.0^\circ} = \frac{23}{\sin 105^\circ} \right) \sin 39.0^\circ$$

2. $B = 38^\circ, b = 4.7, c = 5.9$



$m\angle A = 91.4^\circ / 12.6^\circ$ $a = 7.6 / 1.7$

$m\angle B = 38^\circ$ $b = 4.7$

$m\angle C = 50.6^\circ / 129.4^\circ$ $c = 5.9$

$$\left(\frac{\sin C}{5.9} = \frac{\sin 38^\circ}{4.7} \right) 5.9$$

$$\sin^{-1} \left(\frac{5.9 \sin 38^\circ}{4.7} \right)$$

$$\left(\frac{a}{\sin 91.4^\circ} = \frac{4.7}{\sin 38^\circ} \right) \sin 91.4^\circ$$

$50.6^\circ > 38^\circ$
so 2 Δ

2nd Δ
 $180^\circ - 50.6^\circ = 129.4^\circ$
 $180^\circ - 38^\circ - 129.4^\circ$
 $\left(\frac{a}{\sin 12.6^\circ} = \frac{4.7}{\sin 38^\circ} \right) \sin 12.6^\circ$

3. $m\angle B = 61^\circ, m\angle C = 108^\circ, a = 5 \text{ yd}$

$m\angle A = \underline{\hspace{2cm}}$ $a = \underline{\hspace{2cm}}$

$m\angle B = \underline{\hspace{2cm}}$ $b = \underline{\hspace{2cm}}$

$m\angle C = \underline{\hspace{2cm}}$ $c = \underline{\hspace{2cm}}$

4. $m\angle C = 36^\circ, b = 19 \text{ m}, c = 20 \text{ m}$

$m\angle A = \underline{\hspace{2cm}}$ $a = \underline{\hspace{2cm}}$

$m\angle B = \underline{\hspace{2cm}}$ $b = \underline{\hspace{2cm}}$

$m\angle C = \underline{\hspace{2cm}}$ $c = \underline{\hspace{2cm}}$

Steps for solving Application Problems

- 1) Read the problem
- 2) Define a variable
- 3) Write an equation
- 4) Solve the equation
- 5) Check your answer

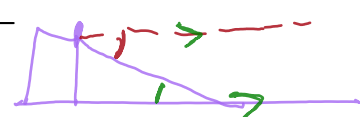
Complementary angles— *add 90°* 

Supplementary angles— *add 180°*

How to solve if have 2 sides and a right angle— *Pythag theorem*

Triangle sum theorem— *add 180°*

Angle of elevation—  *inside Δ*

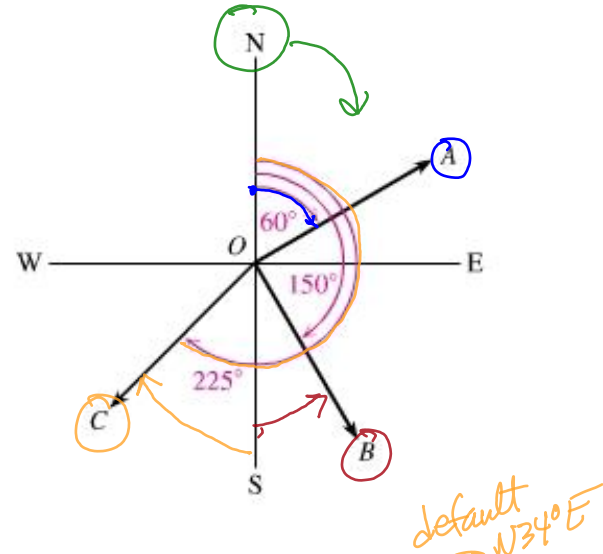
Angle of depression—  *outside Δ*

Line of sight—

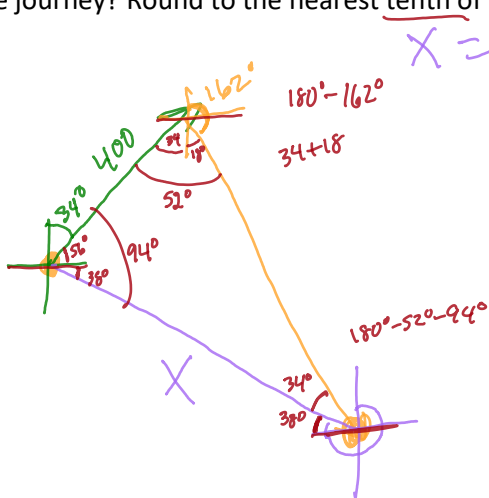
Bearing: The measure of an angle that describes the direction of a ray is called the bearing. Bearing is the clockwise angle from due north.

Another way to express bearing is to describe the acute angle that the ray makes with a ray pointing due north or south. For example:

N60°E is a bearing of 60° east of north
 S30°E is a bearing of 30° east of south — *N130°E*
 S45°W is a bearing of 45° west of south
N225°E



Example: During an important NATO exercise, an F-14 Tomcat left the carrier Nimitz on a course with a bearing of 34° and flew 400 miles. Then the F-14 flew for some distance on a course with a bearing of 162°. Finally, the plane flew back to its starting point on a course with a bearing of 308°. What distance did the plane fly on the final leg of the journey? Round to the nearest tenth of a mile.



X = distance of final leg

$$\left(\frac{X}{\sin 52^\circ} = \frac{400}{\sin 34^\circ} \right) \sin 52^\circ$$

$$X \approx 563.7 \text{ mi}$$