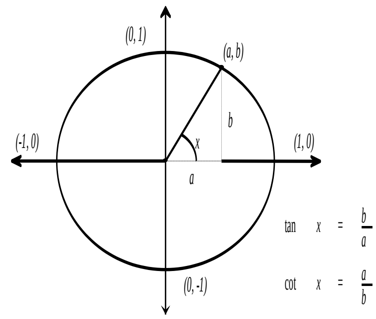
SM 3H

Date: **Section:**

Objective:

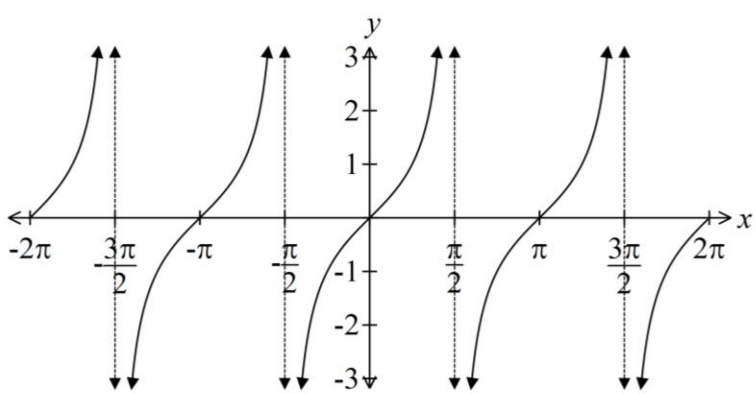
Let (a,b) be coordinates of points on the unit circle. For any given angle *x*, $\tan x = b/a$. This means that $y = \tan x$ is undefined whenever $a = 0$. For any given angle *x*, $\cot x = a/b$. This means that $y = \cot x$ is undefined whenever $b = 0$. Notice that it takes π radians for the values of the tangent and cotangent to make one complete cycle.



Graphing Tangent Functions:
The domain of $y = \tan x$ is the set of all real numbers except numbers of the form____________ where *k* is an integer. The equations of the vertical asymptotes are ___________________ where *k* is an integer.

Key points on the graph of $y = \tan x$:

x					
$y = \tan x$					



To graph $y = a\tan\left[b\left(x-c\right)\right]+d$:

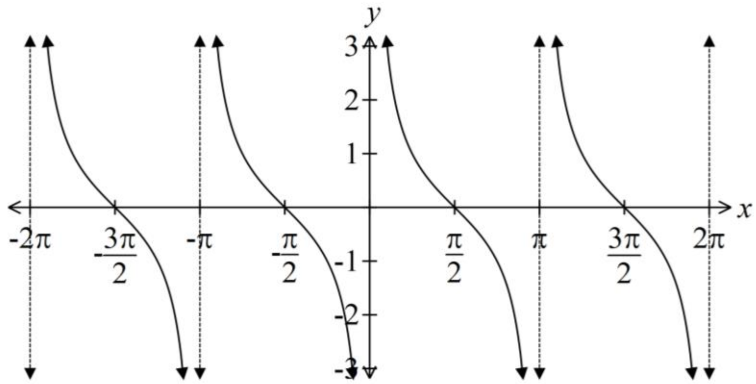
1. Start with the three key points on the graph of $y = \tan x$ and the equations of the asymptotes.
2. Find three key points and the asymptotes for $y = a\tan\left[b\left(x-c\right)\right]+d$ by:
    a. dividing each *x*-coordinate by *b* and adding *c*. (Treat the equations of the asymptotes like *x*-coordinates.)
    b. multiplying each *y*-coordinate by *a* and adding *d*.
3. Sketch one cycle of $y = a\tan\left[b\left(x-c\right)\right]+d$ through the three new points and approaching the new asymptotes.

★ **The period of $y = a\tan\left[b\left(x-c\right)\right]+d$ and $y = a\cot\left[b\left(x-c\right)\right]+d$ is ________ rather than $2\pi/b$.**

Graphing Cotangent Functions:
The domain of $y = \cot x$ is the set of all real numbers except numbers of the form ________ where k is an integer. The equations of the vertical asymptotes are __________ where k is an integer.

Key points on the graph of $y = \cot x$:

x					
$y = \cot x$					

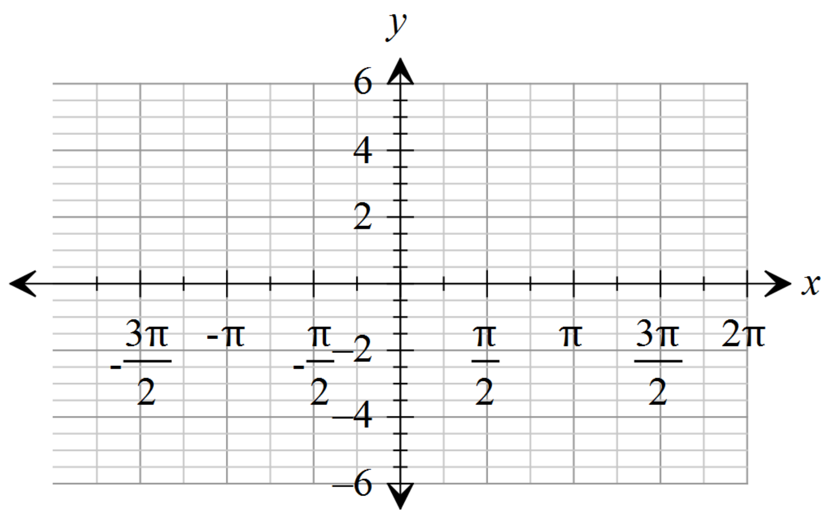


To graph $y = a\cot\left[b\left(x-c\right)\right]+d$:

1. Start with the three key points on the graph of $y = \cot x$ and the equations of the asymptotes.
2. Find three key points and the asymptotes for $y = a\cot\left[b\left(x-c\right)\right]+d$ by:
   a. dividing each x-coordinate by b and adding c. (Treat the equations of the asymptotes like x-coordinates.)
   b. multiplying each y-coordinate by a and adding d.
3. Sketch one cycle of $y = a\cot\left[b\left(x-c\right)\right]+d$ through the three new points and approaching the new asymptotes.

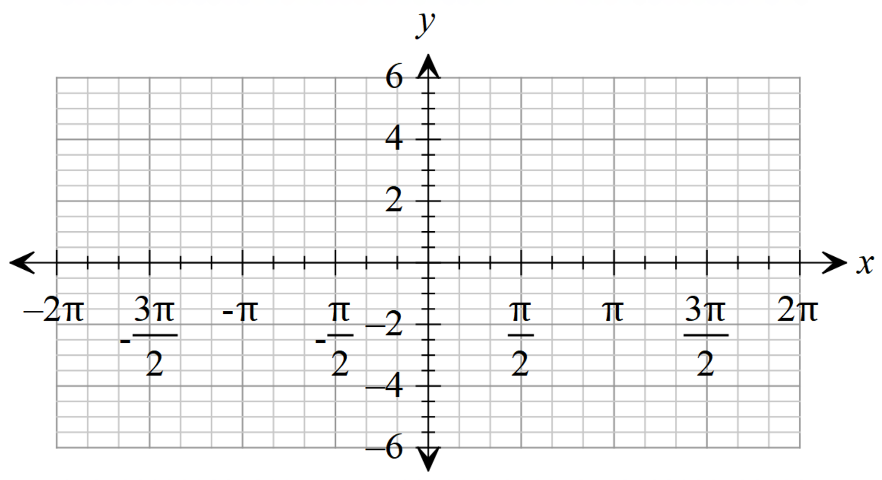
Examples: Graph the following functions. Find the period and the equations of the asymptotes of each.
$f(x) = \tan\left(\frac{1}{2}x\right)$

x	f



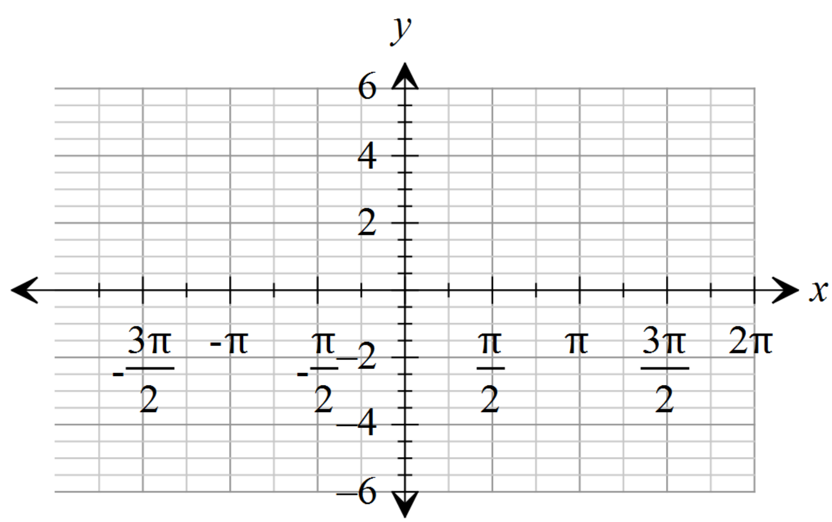
$f(x) = 2\cot\left(x + \frac{\pi}{3}\right)$

x	$f(x)$



$f(x) = 3\tan\left(2x + \frac{\pi}{2}\right) + 1$

x	$f(x)$



$f(x) = 2\cot\left[3\left(x - \frac{\pi}{6}\right)\right] - 1$

x	$f(x)$